

Equations of motion

- $V_1 = V_0 + at$
 - v is velocity (units m/s)
 - a is acceleration (unit m/s^2)
 - t is time (units seconds)

- the final velocity equals the initial velocity + time \times acceleration

- if we integrate this equation with respect to time we get:

- $X_1 = X_0 + \frac{1}{2} at^2 + V_0t$

- the final position of the object equals the initial position + $\frac{1}{2} at^2 + V_0t$

Equations of motion

- $V^2 = U^2 + 2a(X_1 - X_0)$
- final velocity V^2 equals the initial velocity $U^2 + 2 \times$ the acceleration \times the difference in position
- $X_1 = X_0 + \frac{1}{2}(V + U)t$

Equations of motion

- $F = ma$
- force in Newtons ($\text{Kg } m/s^2$)
- the force required to accelerate one kilogram of mass at the rate of one metre per second squared
 - Saturn V rocket generated 34.5 million newtons (lift off) !
 - the translunar injection burn propelled the rocket to 10408 m/s (23286 miles per hour)

Hookes Law

- $F = -k(l_1 - l_0)$

- the force is equal to $-k \times$ the current position of the spring - the at rest position of the spring
 - l_0 at rest position of the spring
 - l_1 current position of the spring
 - k is the spring constant

Hookes Law

- $F = ma$

- $a = \frac{F}{m}$

- $a = \frac{-k(l_1 - l_0)}{m}$

PGE and springs

- examine the example code (<https://github.com/gaiusm/pge/blob/master/examples/springs/simple.py>)
- creates a two circles, one is fixed, one is moving and a spring between them
 - in function main
- <https://github.com/gaiusm/pge/blob/master/examples/springs/simple.py>

```
first = placeBall (wood_light, 0.55, 0.95, 0.03).fix ()  
second = placeBall (wood_dark, 0.55, 0.35, 0.03).mass (1.0)  
s = pge.spring (first, second, 100.0, 3.0, 0.5).draw (yellow, 0.005)
```

PGE and springs

- the parameters to the `spring` method are:
 - `first` object
 - `second` object
 - spring constant ($k = 100.0$)
 - damping constant ($d = 3.0$)
 - at rest length ($l = 0.5$)
- if the at rest length is omitted then it is assumed that the distance between `first` and `second` is the at rest value

Spring damping value

- $F_s = -k_s(l - r)$
 - F_s is the force of the spring
 - k is the Hookes constant of the spring
 - l is the current position of the spring
 - r is the at rest position of the spring

- if we model the spring using this equation, the spring will bounce an object forever
 - we need a method to extract energy out of the spring, to give it realism

Spring damping value

- $F_d = -k_d(v_1 - v_2)$
 - F_d is the damping force
 - k is the hookes value of the damping value of the spring
 - v_1 is the velocity of object 1 at the end of the spring
 - v_2 is the velocity of object 2 at the other end of the spring

Spring damping value

- finally these two equations are joined together
- $F_1 = -(k_s(l - r) + k_d((v_1 - v_2) \cdot L)/l)L/l$
- F_1 is a scalar overall force of the spring at the current position
 - k_s is the Hookes constant for the spring
 - k_d is the Hookes damping constant for the spring
 - v_1 and v_2 are vectors of the velocity of the two objects connected by the spring
 - L is a vector of the positional difference between the two objects
 - l is the distance between the two objects

Spring damping value

- notice the dot product, which for a vector of two items is equal to:
- $a \cdot b = a_0 \times b_0 + a_1 \times b_1$
- the input parameters to a dot product operator are vectors and the result is a scalar
- the force acting on object 1 is F_1
- the force acting on object 2 is $F_2 = -F_1$

Springs in PGE

- take a look at the example [bridge.py](https://github.com/gaiusm/pge/blob/master/examples/springs/bridge.py) (`https://github.com/gaiusm/pge/blob/master/examples/springs/bridge.py`) which implements a simple bridge using 4 non fixed circles and 5 springs
- notice that PGE allows us to define a callback for a spring when it reaches a length
 - in the `bridge` example a spring will snap when it reaches `snap_length (0.16)`